150 million years of sustained increase in pterosaur flight efficiency

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Summary

The long-term accumulation of biodiversity has been punctuated by remarkable evolutionary transitions that allowed organisms to exploit new ecological opportunities. Mesozoic flying reptiles – the pterosaurs – which dominated the skies for over 150 million years (myr) were the product of one such transition. The ancestors of pterosaurs were small and likely bipedal early archosaurs[1], which were certainly well adapted to terrestrial locomotion. Pterosaurs diverged from dinosaur ancestors in the Early Triassic (~245 myr ago, Ma), and yet their first fossils come 25 myr later, in the Late Triassic. Thus, in the absence of proto-pterosaur fossils, it is difficult to study how flight first evolved in this group. Our aim here is to study the evolutionary

dynamics of pterosaurs' adaptation to a new locomotory medium. The earliest known pterosaurs took flight and subsequently appear to have become capable and efficient flyers. However, it seems clear that transitioning between forms of locomotion[2,3] - from terrestrial to volant – challenged early pterosaurs by imposing a steep energetic hill to climb, thus requiring flight to provide some offsetting fitness benefits. Using novel phylogenetic statistical methods and biophysical models combined with information from the fossil record, we detect an evolutionary signal of natural selection acting to increase flight efficiency over millions of years. Our results show that there was still significant room for improvement in terms of efficiency after the appearance of flight. However, in the Azdarchoidea[4], a clade exhibiting gigantism, we test the hypothesis that there was a decreased reliance on flight[5-7] and find evidence for reduced selection on flight efficiency in this clade. By combining biophysical models and phylogenetic statistical methods with the fossil record, we offer a blueprint to study functional and energetic changes through geological time objectively at a far more nuanced level than has ever before been possible.

In order to determine how pterosaurs' propensity for flight changed during their evolutionary history, we calculated two indices of flight performance using a biophysical model of powered and gliding flight[8-10]. Firstly, we used an efficiency of flight index (kg m J^{-1}), that is the inverse of the cost of transport[10], CoT^{-1} (see Methods and Table S1 for the flight model parameterization). The CoT (J $kg^{-1}m^{-1}$) is the metabolic energy required to move a unit mass a unit distance at the least energetically expensive travel speed. Secondly, we calculated a sinking rate[10], V_z (m

49 s^{-1}, see Methods) valid for gliding. A low sinking rate allows for longer travel
50 distances per glide, but also for climbing in updrafts where sinking rate must be
51 lower than the rate at which air rises from the ground. Both CoT^{-1} and V_z were
52 calculated using published estimates of mass[11,12], wingspan[13], wing area[11,12], and
53 projected frontal area[12]. The dataset we use in this paper has mass and wing area
54 estimates for 16 species of pterosaur[11] (Table S2, Methods). Although an alternative
55 dataset of mass and wing area estimates is available for 12 species[12], the two
56 datasets cannot be combined owing to considerable differences in the approaches of
57 each paper to body mass estimation (and the fact that the two datasets overlap).
58 However, our results are qualitatively the same using mass and wing area estimates
59 from each of the two datasets in isolation, and so here we only report the results
60 from one dataset[11]. We use published frontal areas[12] and wingspans[13] (see Methods
61 for details).
62 Studying the changes in CoT^{-1} and V_z through time can inform us about how
63 evolutionary changes such as natural selection have acted on flight performance
64 throughout the course of pterosaur evolution. The lack of proto-pterosaurs in the
65 fossil record means that it is currently impossible to be sure how the pterosaurs
66 initially overcame the energetic hill necessary to achieve flight. Our aim is to study
67 the evolutionary dynamics of pterosaurs' adaptation to a new locomotory medium.
68 The earliest known pterosaur fossils indicate they were able to fly[14]. If during their
69 150 myr of evolution their flight performance and efficiency did not improve or
70 decrease we would expect to see no trend in CoT^{-1} and V_z over time (Figure 1a). We
71 might however expect that after the start of a transition involving a change in the
72 defining medium of locomotion (i.e. from terrestrial to volant), species would be
73 relatively energetically inefficient at moving in the new environment. Thus, over time

74 they would become more efficient. In this case, we would expect flight efficiency
75 (CoT^{-1}) to increase through time and sinking rate (V_z) to decrease (Figure 1b). We
76 would expect the opposite (a decrease in CoT^{-1} and an increase in V_z over time) if
77 flight performance reduced over time (Figure 1c).

78 In order to study the evolution of flight (including calculation of the flight
79 performance indices), it is necessary to account for shared ancestry owing to
80 phylogeny. Several phylogenetic trees for pterosaurs exist in the literature [e.g. 1,15,16],
81 but none of these provides well-justified estimates of the uncertainty among species
82 relationships and divergence dates. To account for phylogenetic and temporal
83 uncertainty in our analyses we constructed a Bayesian dated posterior sample of
84 phylogenetic trees for 128 pterosaurs using published character state data[15] (Figure
85 2, Supplementary Data 1, and see Methods).

86 Wingspan is strongly associated with pterosaur morphologies. We find
87 wingspan explained 97% (range of the posterior distribution, 95–98%) of the
88 variation in mass, 97% (96–98%) of the variation in wing area, and 75% (71–87%) of
89 the variation in frontal area. Then using a phylogenetic prediction method[18] we
90 derived a posterior distribution of imputed masses, projected frontal area and wing
91 area for a further 59 species of pterosaurs based on the results of the phylogenetic
92 regression analyses and our phylogenetic tree (Table S2). Our use of Bayesian
93 phylogenetic methods means we integrate our analyses over all phylogenetic
94 (topology and divergence dates) and model uncertainties. Thus, based on our
95 imputations, we calculated a posterior distribution of 1000 CoT^{-1} and 1000 V_z
96 estimates for use in our analyses of flight performance through time (see Methods).
97 These imputations are robust to jack-knife re-sampling (see Extended Data Figure
98 1). Our final set of analyses used information from 75 species, including the

uncertainty from imputed values that span the majority of the phylogenetic diversity of all known pterosaurs (Figure 2a).

While CoT^{-1} is an efficiency index related to the amount of energy needed to travel a given distance, independently of how long it takes, we do expect it to correlate with mass[19]. It is energetically cheaper for a large animal to move a given mass over a particular distance than for a small animal to travel the same distance[20] (Figure 2b). Sinking rate is similarly affected by mass (Figure 2c) and reflects the relationships we know for birds and bats (Extended Data Figure 2, Supplementary Information).

This relationship with mass means that we need to simultaneously consider mass and its evolutionary association with flight performance in our analyses of flight efficiency and sinking rate through time. With this in mind, pterosaurs have been reported to conform with the well-known Cope's rule[13] – a phenomenon where species increase in size through geological time. The most compelling evidence for this is derived from analyses reporting an increase in wingspan from ~150 Ma to the end of the Cretaceous (~66 Ma) coincident with the origin of birds (Avialae)[13]. However, such a trend could emerge as a consequence of increased flight efficiency rather than increase in body size *per se*. Animals with a larger wingspan for their mass are likely to be more efficient flyers[9]. We find using a phylogenetic regression model that accounts for the uncertainty in our inferred tree and our estimates of species masses, frontal area and wing area (see Methods), that pterosaur size did increase significantly through time. In addition, a model that allows the rate of mass increase through time to differ before and after the origin of the birds fits significantly better than a model without such an inflection. In line with earlier conclusions[13], we find that there is no significant increase in size until ~150 Ma ($p_x = 0.59$). From that

point the average pterosaur grew significantly from 0.60 kg to 6.05 kg (proportion of the posterior distribution that crosses zero, $p_x = 0.02$), a ~10-fold increase in size, over 65 million years.

Turning now to flight performance, there is a growing body of evidence indicating that the Azhdarchoidea had strong terrestrial affinities[5-7,21] (cf. [22]). Here the Azhdarchoidea are considered to comprise the common ancestor and all descendants of *Tapejara, Quetzlcoatlus,* and *Dsungaripterus*[1] (posterior nodal support = 0.83 in our phylogeny). Evidence suggests that azhdarchoid pterosaurs had relatively inflexible necks[7], left tracks indicating terrestrial proficiency[5], and possessed other adaptations associated with ground-dwelling generalist foraging (reviewed[6,7]). Dsungaripterids (the most basal azdharchoids in our phylogeny, Figure 2) are reported to have been wading foragers[14,21] feeding on hard-shelled organisms at water margins[23]. Given the terrestrial tendencies in the Azhdarchoidea compared to what we know about other pterosaurs, we might expect diminished reliance on flight, leading to the expectation that they might have differed from other pterosaurs in the selection pressures for adaptations associated with flight and locomotion. Thus, in our analyses we test whether the evolution of flight performance through time in the Azhdarchoidea is distinct from other pterosaur species.

Applying phylogenetic regression to flight efficiency through time we find that, even after accounting for mass, efficiency increased significantly ($p_x = 0.00$, Figure 3a–c) in non-azdarchoid pterosaurs. However, in contrast to our finding for mass, there is no significant effect associated with the arrival of birds ($p_x = 0.47$). Early pterosaurs (<200 Ma) had an average efficiency of 0.29 kg m J^{-1} but by 70 Ma they were greater than 50% more efficient (CoT^{-1}= 0.51 kg m J^{-1}). Congruently we find that sinking rate (after accounting for mass) for non-azdarchoid pterosaurs reduced

from 0.80 m s^{-1} to 0.50 m s^{-1} over the course of the 150 myr of their evolutionary history (Figure 3d–f). In contrast, azdarchoids exhibited no change in efficiency or sinking rate from origin to extinction.

Our results show that, save for azdarchoids, following their transition to volant locomotion, the pterosaurs exhibited a sustained increase in flight efficiency over 150 myr until their extinction. To achieve this, natural selection acted to decouple the evolution of body size and wingspan (Figure 3g–i) to sculpt these enigmatic creatures from what might have been inefficient flyers that took to the air for only short spells, to creatures that could fly long distances over extended periods. At their origin, some ~147 Ma, 85 myr after the origin of crown pterosaurs, azdarchoids had a slightly lower flight efficiency and higher sinking rates compared with their contemporaries – and showed no temporal trends in either trait until their eventual extinction (Figure 3a–f). This reduced pattern of flight efficiency is also borne out in analyses of gross morphology - azdarchoids arose with short wings for their size, and maintained this condition until their final demise.

Our approach demonstrates the power of combining biophysical models and phylogenetic statistical methods with the fossil record to understand the evolution of flight in pterosaurs. In doing so we offer a blueprint to study functional and energetic changes objectively through geological time at a far more nuanced level than has ever before been possible.

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Figure Legends

Figure 1: Hypothesised scenarios of the evolutionary trajectory of flight performance metrics through time. a) No relationship between flight performance metrics and time would indicate no directional change in flight ability through time. b) An increase in efficiency through time and a reduction in sinking rate would demonstrate a general tendency for selection favouring increased flight performance as the pterosaurs radiated. c) A decrease in efficiency and an increase in sinking rate would imply a reduction in flight performance through time. The branches of the phylogenetic trees are coloured by hypothesised magnitudes of efficiency (green) and sinking rate (blue).

Figure 2: Pterosaur phylogeny and the relationship of flight performance metrics with mass. a) Density diagram [17] showing the uncertainty in our phylogenetic reconstruction for pterosaurs (n=128, see Methods for details). Superimposed is the maximum clade credibility tree and triangle points indicate species for which we have published data on mass, wing area, frontal area, and wingspan. Circle points indicate species for which we have wingspan only. Red denotes azdarchoids. b) The relationship between flight efficiency and mass (n=75),

with our mean phylogenetic imputations plotted with standard deviations shown by the green ellipses. c) The relationship between sinking rate and mass (n=75), with our mean phylogenetic imputations plotted with standard deviations shown by the blue ellipses. Silhouette of Eudimorphodon is taken from phylopic.org and is available for reuse under the Public Domain Dedication 1.0 license (https://creativecommons.org/publicdomain/zero/1.0/), credit to Steven Traver.

Figure 3: Flight performance through time. Summary plots for each of our three main traits of interest (efficiency, a–c; sinking rate, d–f; wingspan, g–i). A phylogeny of the species included in each analysis (a, d, g) is shown with branches shaded by reconstructed trait values; Azdarchoidea is highlighted in red. Trait data are shown plotted against time (b, e, h) where all species with imputed values are represented by circles – excepting wingspan data which is all from published sources. Points are coloured by species' body mass and azdarchoid species are outlined in red. The posterior distribution of model predictions for each trait against time (c, f, i) shows how these traits evolved during pterosaur history. These relationships demonstrate that – after accounting for size – pterosaurs continually increased their efficiency (c) and wingspan (i) whilst there was a continual reduction in sinking rate (f) through time (grey lines, median in black). This applies to all pterosaurs except azhdarchoids (pink lines, median in red) which show no significant trends – although they do have relatively short wings for their mass (i). Silhouette of Eudimorphodon (black) is taken from phylopic.org and is available for reuse under the Public Domain Dedication 1.0 license (https://creativecommons.org/publicdomain/zero/1.0/), credit to Steven Traver. Silhouette representing Azdarchoidea (red) is taken from phylopic.org and is available for reuse under the Creative Commons Attribution 3.0 Unported license (https://creativecommons.org/publicdomain/zero/1.0/), credit to Darren Naish (vectorized by T. Michael Keesey).

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Methods

Phylogenetic Inference

All morphological data were obtained from a published phylogenetic character matrix[15]. However, we retained only discrete morphological characters, excluding the continuously varying characters, and treating all ordered characters as unordered, resulting in a total of 220 discrete morphological characters coded for 128 pterosaur species.

We constructed a posterior sample of time-calibrated phylogenetic trees for pterosaurs using the birth-death serial-sampling model[24,25] as implemented in BEAST v2.4[26] allowing for simultaneous estimation of both the topology and divergence times. For each species, we tip-dated using the midpoint of the stratigraphic age representing the first appearance of each species using published time intervals[1,13,15]. The origin of the birth-death process was estimated from a uniform prior distribution ranging from the age of the youngest species in the tree (*Eudimorphodon rosenfeldi*) up to an arbitrary upper limit of 350 Ma.

Owing to the lack of information about speciation and extinction rates in the pterosaur literature we took a conservative approach by placing a wide uninformative prior distribution (uniform ranging between 0 and infinity) on both the effective reproductive number (the birth-death ratio) and the “become uninfectious rate” (total death rate). Similarly, we placed an uninformative uniform prior between 0 and 1 on the sampling proportion. Together, these parameters enable direct estimation of birth-death rates throughout the phylogenetic tree[24].

We modelled rate heterogeneity across lineages using an uncorrelated relaxed morphological clock[27]. We placed an exponential prior (mean = 1) on the mean of the lognormal distribution from which the branch-wise clock rates are drawn,

297 and a gamma prior (α = 0.5396, β = 0.3819) on the standard deviation. Characters
298 were partitioned on the basis of the number of discrete states, and we applied Lewis'
299 Markov k (Mk) model of morphological character evolution[28] across all partitions,
300 estimating a shared gamma shape parameter (Γ_4)[29] using an exponential prior
301 distribution with mean = 1.
302 The MCMC chain was run for one billion iterations, sampling every 100,000
303 iterations after convergence. To produce the posterior sample of 1,000 phylogenetic
304 trees used in the main analyses, we randomly sampled 1,000 iterations from this
305 chain, ensuring that all parameters had an effective sample size of >500, calculated
306 using Tracer v1.6[30]. We ensured that all parameters that were estimated using a
307 uniform uninformative prior (origin, effective reproductive number, become
308 uninfectious rate, and the sampling rate) returned a posterior distribution of
309 estimates that differed from the prior. The analysis was repeated multiple times to
310 ensure convergence was reached. All chains were inspected visually using Tracer
311 v1.6[30].
312 The full sample is visualized in Figure 2a as a density tree produced in R[31]
313 using functions available in the package phangorn[17], and is available to download in
314 nexus format as Supplementary Data 1 of this article.

315 *Imputation of pterosaur measurements*
316 To calculate our efficiency index (see below) we required mass, frontal area and
317 wing area for adult pterosaur species. Estimates for mass and wing area are
318 available for N=16 species from Witton [11] and N=12 species from Henderson [12] (see
319 Table S2). For frontal area values are taken from Henderson [12] (N = 12, though see
320 below). Independently for each of the two datasets, we used the phylogenetic
321 method outlined in[18] to impute a posterior sample of 1000 estimates of mass, frontal

area and wing area for a total of N = 75 species. We obtained wingspans for additional species from[13] (a list of species used is found in Table S2) and used each morphological trait's relationship with wingspan (i.e. a phylogenetic regression of each trait against wingspan) to impute species-specific values. As a part of this procedure, we also imputed frontal area for the N=7 species in the Witton [11] dataset which did not have data in Henderson [12] (see Table S2).

Flight energetics model

Animal powered flight energetics, while perhaps kinematically different for bats, birds and pterosaurs, are still ultimately constrained by physics. It has previously been demonstrated that it is possible to infer flight performance of pterosaurs using biophysical models of flight in combination with metabolic scaling estimates from birds[8]. Here we used an actuator-disc based model owing to the pedigree of this approach and because more complex wake dynamics models and computational approaches are particularly difficult to parameterize, requiring a number of kinematic parameters such as wingbeat frequency that are impossible to infer from fossil material. We used a modified version of Pennycuick's Flight model (v1.25)[9] that we developed from earlier work[8] and implemented in Matlab®[32], and which includes published parasite power estimates[33]. Flight performance is estimated based on morphological measurements such as body mass, wingspan and wing area (Table S1) and the model produces a U-shaped power-to-airspeed relationship, from which a minimum power speed (V_{mp}) can be calculated. This V_{mp} is the least energetically expensive flight speed and so provides a useful proxy for efficiency[10] when incorporated into the CoT.

We used the model to estimate the metabolic and mechanical power required for powered (flapping) flight given information on a minimal set of morphological

traits and estimates of physiology, as well as aerodynamic constants (Table S1). The intersection of the power curve with an animal's available metabolic power (P_{BMR}, calculated from mass and estimated basal metabolic rate, BMR) allows us to characterise flight ability[9,34]. Consistent with current thought[35,36], and in line with previous studies[8], we assume that pterosaurs had a BMR similar to that of birds.

Estimation of energetic efficiency

A number of energetic efficiency measures exist[10] but one useful proxy is the inverse of the mass specific Cost of Transport (CoT, the energy required to move a unit mass a unit distance, independent of the time taken to do so). We estimate CoT as $P_{BMR}/(V \times M)$ where V is the least energetically expensive travel speed (i.e. V_{mp}) and other parameters are as in Table S1.

For species with available data (Table S2) we produced a single estimate of CoT^{-1} using the inverse of the above formula. For each of the species for which we imputed mass, frontal area and wing area (Table S2 and above), we use the full sample of our imputed values to produce a posterior sample of 1000 estimates of CoT^{-1}.

As formulated, CoT accounts for mass. However, as energy efficiency appears to increase with body size[19,20] we included size in our regression model of CoT^{-1} through time (main text and see below) to account for this.

Estimation of sinking rate

Sinking rate while gliding (V_z) was calculated as $D \times V_{mp} / M \times g$ (where D is the total aerodynamic drag resulting from the addition of the induced, parasite and profile drags) and assuming a linear wingspan reduction (see[34]).

Phylogenetic regression models testing temporal trends in mass and efficiency

To test the evolutionary trajectories of pterosaur mass and measures of flight efficiency through time we use phylogenetic generalized least squares[37,38] multiple regression models in a Bayesian framework. We assessed the significance of regression parameters using the proportion of the posterior distribution that crosses zero, p_x, where we consider $p_x < 0.05$ as significant. In addition to the 16 species for which we have single estimates of body mass, V_Z and CoT^{-1} from[11] (or N = 12 from[12]), in all our models we include the full set of posterior estimates of both body mass and CoT^{-1} for all species for which the data are imputed (Table S2). These values are sampled in proportion to their probability during the running of the MCMC chain. This allows us to incorporate information about the variance of our imputations, avoiding problems associated with summarizing the posterior distribution into a single point estimate.

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Author Contributions

C.V and S.H. conceived the study. C.V., J.B., M.B., and S.H. collected the data. C.V., J.B., A.M., and S.H. conducted the phylogenetic and biophysical analyses. C.V., J.B., A.M., M.B. and S.H. interpreted the results and wrote the paper.

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The authors declare no competing financial interests.

Data Availability Statement

The phylogeny we generated in this study (presented in Figure 2a) is included as Supplementary Information (Supplementary Data File 1) with this article. No other data was generated or analysed during the current study. All data used are available from published sources and are cited in the main text where appropriate.

Software and Code

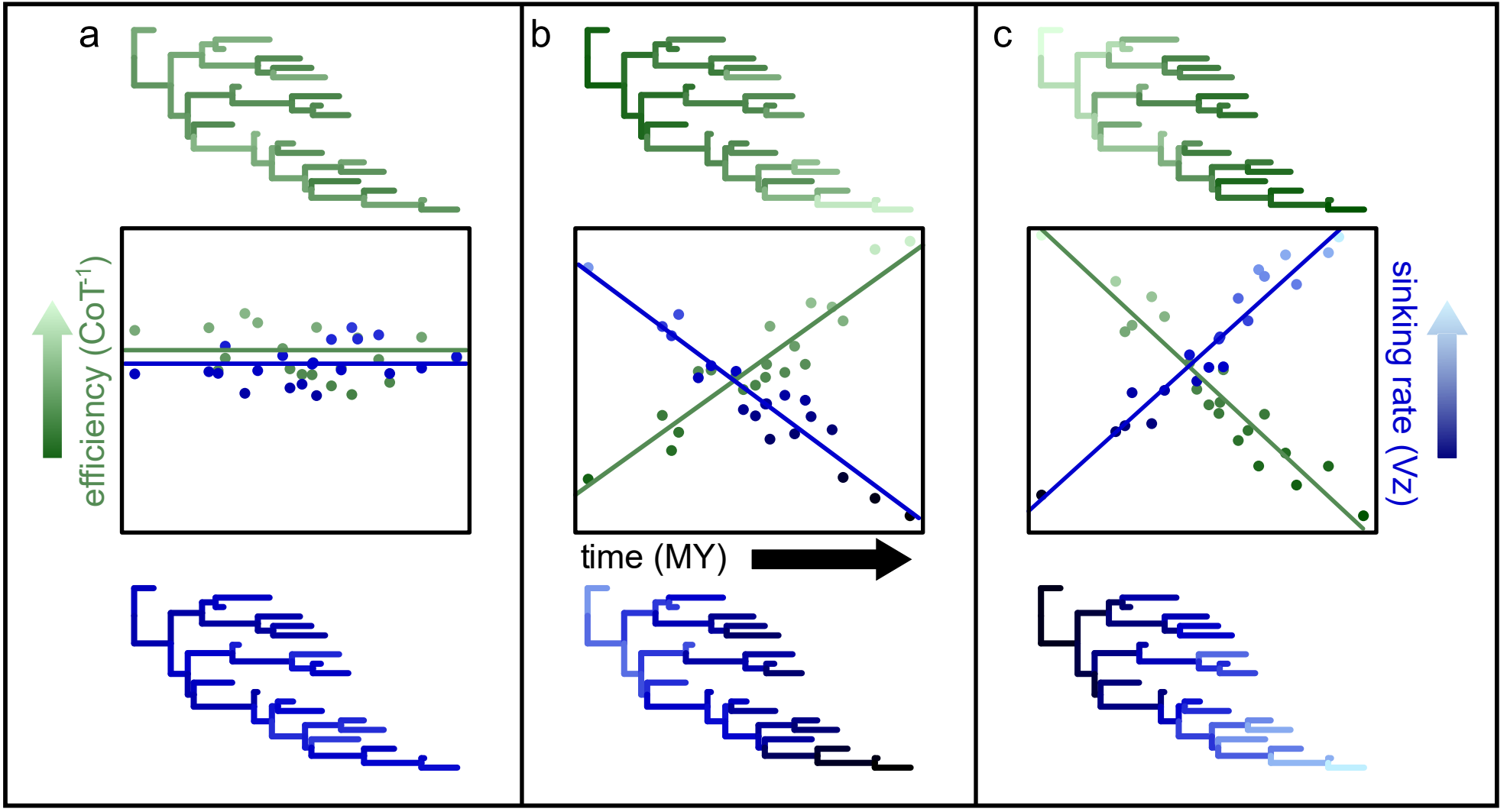
All analyses in this research were conducted using readily available, published programs and are cited in the text. Version numbers of the programs we used are as follows: Tracer v1.6. (2015), MATLAB v9.2 (2017), R v3.4.4 (2017), BEAST 2 (2014), BayesTraits v3 (2018).

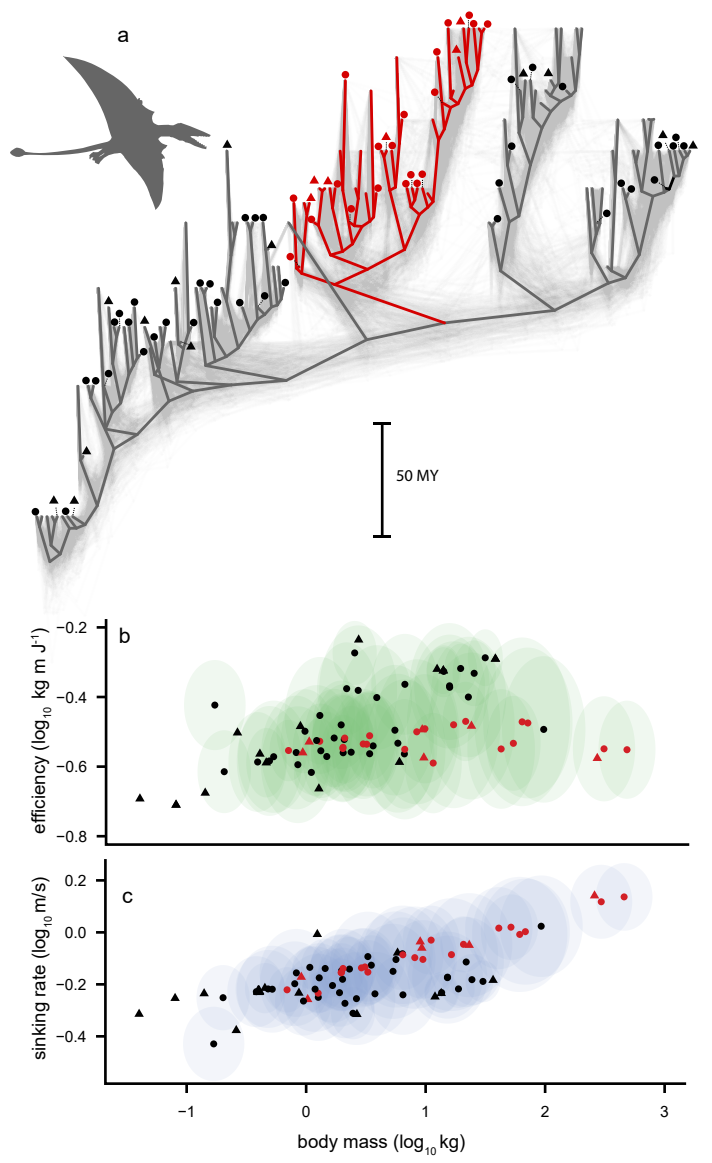
Extended Data Legends

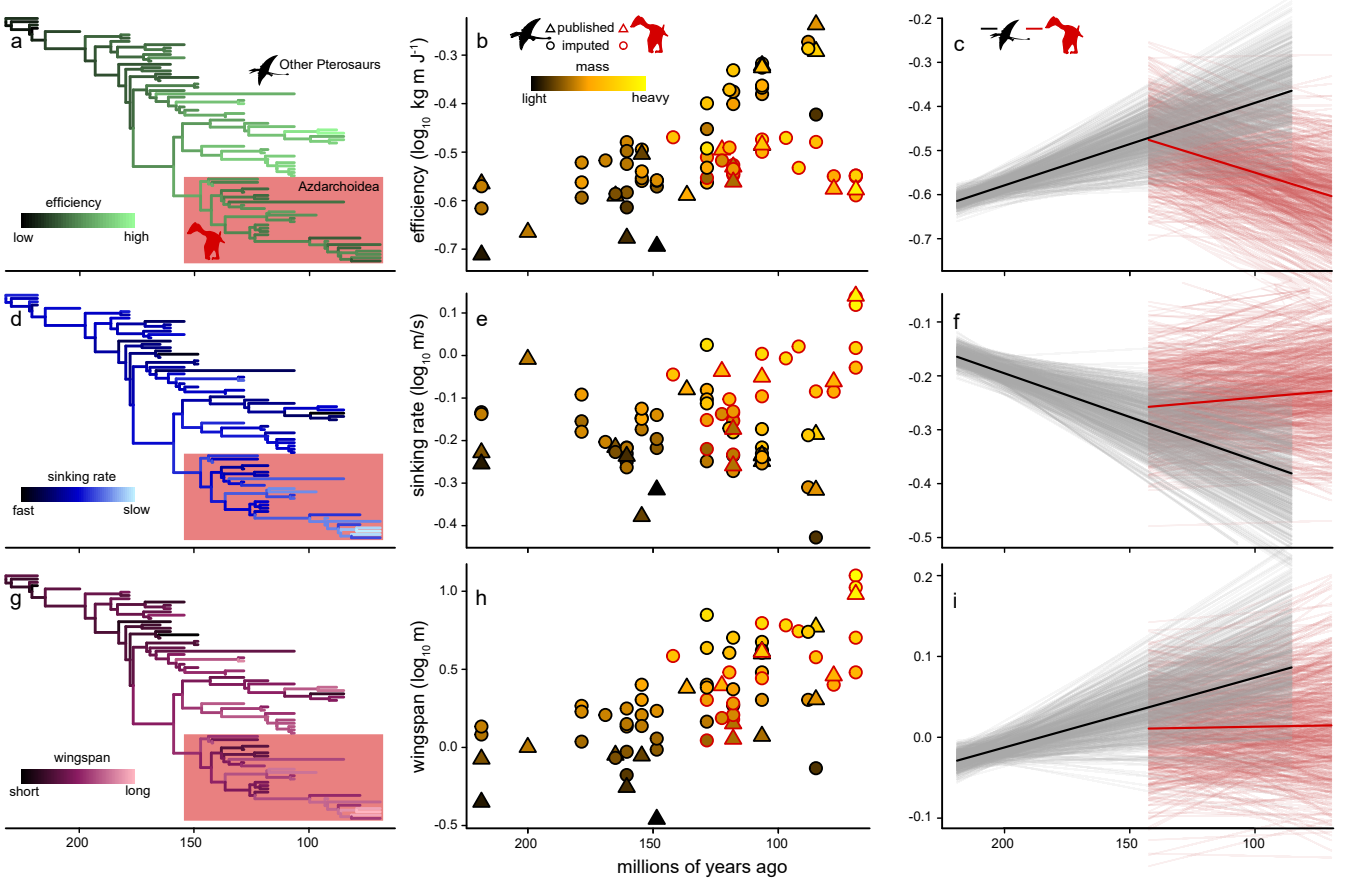
Extended Data Figure 1: Results of our N-1 jack-knife procedure for the mass (a) and wing area (b). Each point represents an individual species. We compare the imputed values for each species from our phylogenetic imputation procedure where that species has been excluded to the published value.

Extended Data Figure 2: Comparison of flight performance metrics between pterosaurs and extant bats and birds. In (a) we show the relationship between flight efficiency and mass in pterosaurs (as in Figure 2b, main text), with our mean phylogenetic imputations plotted with standard deviations shown by the green ellipses. We superimpose a previously reported relationship between flight efficiency and mass for extant birds (orange line), as well as data points for six bat species

(blue crosses). In (b) is the relationship between sinking rate and mass for pterosaurs (as in Figure 2c, main text), with our mean phylogenetic imputations plotted with standard deviations shown by the blue ellipses. Superimposed, we show the range of the relationship between sinking rate and mass for Procellariiformes (orange box) and Accipitriformes[7] (violet box) and individual data points for six specimens of an extinct Cretaceous bird (*Sapeornis chaoyangensis*) (orange quartered circles), 11 extant bird species (orange crosses), and seven bat species (blue crosses). Triangles indicate pterosaur species for which we have published data on mass, wing area, and wingspan. Circles indicate species for which we have wingspan only. All azdarchoids are coloured in red.


a
b
c
efficiency (CoT-1)
time (MY)
sinking rate (Vz)


a
50 MY
b
efficiency ($\log_{10}$ kg m J^{-1})
−0.2
−0.4
−0.6
−0.8
c
sinking rate ($\log_{10}$ m/s)
0.2
0.0
−0.2
−0.4
−1
0
1
2
3
body mass ($\log_{10}$ kg)


a
Other Pterosaurs
Azdarchoidea
efficiency
low
high
b
published
imputed
mass
light
heavy
efficiency (log10 kg m J-1)
c
d
sinking rate
fast
slow
e
sinking rate (log10 m/s)
f
g
wingspan
short
long
h
wingspan (log10 m)
i
200
150
100
millions of years ago